

# ФИЗИКА. АСТРОНОМИЯ СЕРИЯСЫ/ PHYSICS. ASTRONOMY SERIES / СЕРИЯ ФИЗИКА. АСТРОНОМИЯ

IRSTI 29.19.03 Scientific article DOI: https://doi.org//10.32523/2616-6836-2024-148-3-23-40

# Ab-initio calculations for the search for stable structures for iron-phosphorus and nickel-phosphorus systems

A.B. Bazarbek\*<sup>10</sup>, A.D. Akylbekova<sup>10</sup>, G.D.Kabdrakhimova<sup>10</sup>, A.Sh. Omarkhan<sup>10</sup>, A.A. Nogai<sup>20</sup>

<sup>1</sup>L.N. Gumilyov Eurasian National University, Astana, Kazakhstan <sup>2</sup>Kazakh Agro-Technical Research University

(E-mail: asyl.bazarbek.92@mail.ru)

**Abstract.** The study of the internal structure of our planet is one of the most relevant topics in fundamental research. In particular, the analysis of the phase ratios of iron and nickelcompounds with light elements at high pressures is an important task for determining the composition and structure of the core of our planet. Due to the complexity of conducting experiments at such high pressures (in the Earth's core ~365 GPa), ab-initio calculations become a useful method for conducting such studies.

With the advent of new algorithms for searching for crystal structures, such as USPEX, AIRSS and CALYPSO, the number of studies and available data on compounds of iron-nickel-containing systems with light elements has increased significantly. These tools have significantly expanded our capabilities in studying the internal processes in planets, creating broader prospects for further research and understanding the evolution of planetary bodies. The integration of these advanced computational methods makes it possible to accurately predict stable and metastable phases of iron compounds under extreme conditions, providing invaluable data on the behavior of materials in the conditions of the Earth's core.

**Key words:** high pressure physics, ab-initio calculations, quantum chemical modeling, fundamental research, crystal structures.

Received 21.08.2024. Revised 04.09.2024. Accepted 05.09.2024. Available online 30.09.2024

## Introduction

The inner core of the Earth consists of pure iron and its alloy with nickel, as well as impurities of light elements such as hydrogen, carbon, nitrogen, oxygen, silicon, phosphorus and sulfur [1].

Under conditions of high pressure and temperature of the Earth's inner core, iron can undergo phase changes, forming various structures that affect the properties of the core. In addition, the simulation results [2] show that in an iron-phosphorus alloy in the Earth's core, Ni can significantly affect the structure and formation of a solid inner core. The study of the composition and properties of the Earth's core, including the role of an iron-nickel alloy with an admixture of phosphorus, is the key to understanding the dynamics and evolution of our planet [3].

At atmospheric pressure, three intermediate compounds are known in the Fe–P system – FeP,  $Fe_2P$  and  $Fe_3P$  [4]. At atmospheric pressure, FeP has an MnP-type structure, characterized by a *Pnma* spatial group. Gu et al. [5] used the method of X-ray powder diffraction and Mossbauer spectroscopy to study FeP up to 15.6 GPa. This experiment showed that FeP remains in the MnP type structure throughout the considered range.

It was believed that at atmospheric pressure  $Fe_2P$  is represented in the structure of barringerite (P6<sup>-</sup>2m) [6]. However, recent results of an experimental study by Litasov et al. [7] have shown that allabogdanite is a thermodynamically stable polymorphic modification of  $Fe_2P$  at atmospheric pressure.

At atmospheric pressure,  $Fe_{3}P$  has a schreibersite ( $I4^{-}$ ) structure. At high pressures, the structure of schreibersite undergoes changes. Thus, Scott et al. [8, 9] conducted experiments in a diamond cell up to 30 GPa. The authors showed that the schreibersite structure undergoes significant compaction above 8 GPa, and peaks of unidentified structure are observed on the X-ray between 17 and 30 GPa. In addition, according to recent data [10],  $Fe_{3}P$  showed thermodynamic stability up to 40 GPa at high pressure and crystallizes into a tetragonal structure.

At atmospheric pressure, the Ni-P system is characterized by the presence of many phases with different crystal structures [11]: Ni<sub>3</sub>P, Ni<sub>8</sub>P<sub>3</sub>, Ni<sub>12</sub>P<sub>5</sub>, Ni<sub>2</sub>P, Ni<sub>5</sub>P<sub>4</sub>, NiP, NiP<sub>2</sub> and NiP<sub>3</sub>.

However, at high pressures, the amount of data on compounds in the Ni-P system is limited. Dera et al. [12] investigated the behavior of synthetic Ni<sub>2</sub>P in a diamond cell with laser heating at high pressures up to 50 GPa. Under normal conditions, Ni<sub>2</sub>P has a hexagonal structure with P6<sup>-</sup>2*m*symmetry (trans jordan mineral). When compressed without heating, Ni<sub>2</sub>P remains in the P6<sup>-</sup>2*m*structure up to at least 50 GPa. Chornkrathok et al. [13] investigated Ni<sub>3</sub>P in a diamond cell up to pressures of 50 GPa. During the experiments, it was shown that Ni<sub>3</sub>P does not undergo structural phase transitions in the studied pressure range.

The data obtained during such calculations are important for further investigation of the triple Fe–Ni–P system. Therefore, it is important to conduct such studies to establish phase ratios in the Fe-P and Ni-P system at high pressures.

### Methods

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Quantum chemistry is a powerful tool for studying the properties of molecules, crystals, nanostructures and chemical reactions, which is very useful for many fields of science and

technology. Modern methods of quantum chemistry provide an opportunity to describe various chemical and physical characteristics of molecules, as well as the electronic and spatial structure of molecules in solids in their ground state with an accuracy comparable to the data obtained by experimental methods [14].

Quantum chemistry methods allow us to obtain information about the properties of substances that are sometimes unavailable for experimental analysis, especially when it comes to substances under extreme external conditions, such as high temperatures and/or pressures. In such situations, first principles calculation methods, also called ab initio, can be useful. Ab initio methods are based solely on the principles of quantum mechanics and seek to solve the electronic Schrodinger equation, taking into account the position of the nuclei and the number of electrons, in order to obtain the necessary data such as electron density, energy and other properties of the system [15].

Due to the difficulty of conducting an experiment at pressures characteristic of the Earth's core – up to  $\sim 365$  GPa, quantum chemical basic calculations are an effective tool for such studies. Examples of the application of basic calculations are a large number of studies, including data on compounds of iron-nickel alloy with light elements has increased significantly. In particular, calculations were performed to search for intermediate compositions and structures in Fe-C and Fe-H [16], Fe-S [17], Fe-N [18], Ni-S [19], Ni-C [20] systems at high pressures.

Studies of the electronic structure were carried out using density functional theory using the VASP software package [21-23]. The exchange-correlation interaction was taken into account using the generalized gradient approximation, presented in the form of the Purdue-Burke-Ernzerhof (PBE) functional [24]. All calculations included consideration of spin polarization.

For a more efficient search for crystal structures, the USPEX software package [25] was used, which divides calculations into two stages. At the first stage, the search for stable intermediate stoichiometries was carried out, which led to the construction of thermodynamic convex hulls. At the second stage, a search was performed for each fixed stoichiometry represented on the convex hull.

The search for crystal structures was carried out at 0, 100, 200, 300 and 400 GPa. In all calculations for the search for crystal structures, optimization was carried out within the framework of density functional theory using the conjugate gradient algorithm. The calculated parameters were as follows: the cutting energy of plane waves – 400 eV; the density of the Monkhorst-Pack k–point grid [26] – 0.5 Å<sup>-1</sup>; electronic blur – according to the Methfessel – Paxton scheme [27]; smoothing parameter  $\sigma$  = 0.2 eV. Further, the most energetically advantageous structures were optimized at different pressures with higher accuracy, namely, the cutting energy was increased to 600 eV, the density of k-points was 0.2 Å<sup>-1</sup> and the smoothing parameter  $\sigma$  = 0.1 eV.

# Results

To assess the stability of the phases with respect to decomposition into an isochemical mixture, we used the method of constructing a «convex hull» diagram. To create this diagram, it was necessary to know the stable modifications of pure iron and phosphorus, as well as their enthalpies. Within the pressure range from 0 to 13 GPa, our calculations revealed the well-

known BCC modification of pure iron as the phase with the lowest enthalpy. In the pressure range above 13 GPa and up to 400 GPa, the phase with the lowest enthalpy turned out to be GPU-Fe (see Figure 1). This result corresponds well to the experimental data [28-31].



Figure 1 – Dependence of enthalpy on pressure of iron modifications Note – The results are given with respect to the enthalpy of GPU-Fe

In the case of phosphorus, according to the available experimental data, several structural phase transitions under pressure are observed. The most stable form at atmospheric pressure is the so-called black phosphorus, which is characterized by *Cmcasymmetry* and has the structural designation A17 [32]. According to the calculations, the *Cmcastructure* transitions into a trigonal structure with R3<sup>-m</sup> symmetry at 7 GPa (experimental value of 5 GPa [33]) and then into a simple cubic Pm3<sup>-m</sup> at 15 GPa (experiment – 11 GPa [34]). In addition, a phase transition from a simple cubic Pm3<sup>-m</sup> to a simple hexagonal (P6) structure is observed through the intermediate *Cmcm* phase in the pressure range 110-127 GPa (experiment – 107-137 GPa [35]). The *Cmcm* structure is an approximated commensurate model of a disproportionately modulated experimental phase, which is characterized by a four-dimensional supergroup*Cmmm*(00 $\gamma$ )s00 [36, 37]. At a pressure of 205 GPa, the P6 structure transforms into a BCC structure (*Im3<sup>-m</sup>*). Above 299 GPa, the Im3<sup>-m</sup>structure transforms into *I*4<sup>-3</sup>d [38], which is a superstructure of the BCC lattice with small deformations. The I4<sup>-3</sup>dstructure is stable up to 308 GPa, above which the GPU structure is stabilized, which retains its stability to at least 400 GPa. The result obtained is in good agreement with the available experimental studies (Figure 2).



Figure 2 – Enthalpy dependence on pressure of phosphorus modifications Note – All dependencies are shown relative to the enthalpy of modification P6

At atmospheric pressure, three intermediate compounds are known in the Fe-P system – FeP,  $Fe_2P$  and  $Fe_3P$  [39, 40]. Similar phases are observed in experiments and at higher pressures of the order of 23 GPa.

The predicted structures of intermediate compounds in the Fe-P system were used to estimate the enthalpy of formation relative to elementary Fe and P. Figure 3 shows convex hulls constructed in accordance with the structures of iron phosphides found. In the pressure range of 0-400 GPa, three intermediate compounds are stable – FeP, Fe<sub>2</sub>P and Fe<sub>3</sub>P.



a – convex hulls for the Fe–P system at various pressures; b – calculated phase diagram composition-pressure

Figure 3 – Phase stability diagrams in the Fe-P system

Note - Stable structures are indicated by filled blue squares, metastable structures by empty red triangles

FeP undergoes one  $Pnma \rightarrow P2_1/c$  phase transition at 75 GPa. Above 200 GPa, the enthalpy of  $FeP-P2_1/c$  becomes higher than that of  $FeP-P2_13$  (Figure 4). However, up to 400 GPa, the enthalpy difference between these two phases is on average 3-4 meV/f.u. and is within the accuracy of the method (5 meV/f.u.). Thus, it can be said that above 200  $GPaFeP-P2_13$  and  $FeP-P2_1/c$  are equally stable, i.e.they can coexist with each other.



Figure 4 – Enthalpy dependence on pressure of FeP modifications Note – All dependencies are shown relative to the enthalpy of FeP-P2<sup>1</sup>3

Iron phosphide Fe<sub>2</sub>P, according to the calculations carried out, undergoes one phase transition in the studied pressure range. According to our calculations, the structure of barringerite (P6<sup>-</sup>2m) does not have a stability field in the entire studied pressure range, and the stable modification at atmospheric pressure is the structure of allabogdanite, which is characterized by the *Pnma* spatial group (Figure 5). Above 45 GPa, the structure of allabogdanite transitions into a structure that is also characterized by *Pnma* symmetry. Further, we will designate the low-bar modification with the structure of allabogdanite as Fe<sub>2</sub>P-*Pnma-I*, and the high-bar modification as Fe<sub>2</sub>P-Pnma-II. Fe<sub>2</sub>P-Pnma-II is energetically stable up to 400 GPa. It is worth noting that Fe<sub>2</sub>P-*Pnma*-I spontaneously transforms into Fe<sub>2</sub>P-Pnma-II during optimization above 80 GPa. This indicates the structural similarity of these modifications.



Figure 5 – Enthalpy dependence on pressure of  $Fe_2P$  modifications Note – All dependencies are shown relative to the enthalpy of  $Fe_2P-P6^-2m$ 

№3(148)/ 2024 Л.Н. Гумилев атындагы Еуразия ұлттық университетінің ХАБАРШЫСЫ. Физика. Астрономия сериясы ISSN: 2616-6836. eISSN: 2663-1296 In the case of Fe<sub>3</sub>P, the stable modification at atmospheric pressure is the structure of schreibersite with I4<sup>-</sup> symmetry. Above 30 GPa, Fe<sub>3</sub>P-I4<sup>-</sup> passes into a structure characterized by rhombic symmetry Cmcm (Figure 6).



Figure 6 – Enthalpy dependence on pressure of  $Fe_3P$  modifications Note – All dependencies are shown relative to the enthalpy of  $Fe_3P$ -I4<sup>-</sup>

At pressures above 65 GPa,  $Fe_{3}P$  becomes unstable relative to the decomposition reaction  $Fe_{3}P = Fe + Fe_{2}P$  (Figure 7). Iron phosphide  $Fe_{4}P$  is unstable throughout the studied pressure range (Figure 3).



Figure 7 – Dependence of the enthalpy of Fe<sup>3</sup>P on the decomposition into Fe<sub>2</sub>P and Fe

Nickel does not undergo first-order phase transitions within the pressure range under consideration, and the fcc structure has been identified as a stable modification. This result is consistent with experimental data [41]. In contrast, phosphorus, as demonstrated in Figure 2, goes through a series of phase transitions (see Figure 2).

Both predicted and already known structures were used to estimate the enthalpy of formation relative to elementary Ni and P. To assess the stability of intermediate compounds in the Ni–P

system at various pressures, «convex hull»diagrams were constructed in previous work [42]. A number of stable compounds have been identified in thepressure range under consideration.

Nickel phosphides Ni<sub>14</sub>P, Ni<sub>12</sub>P, Ni<sub>10</sub>P, Ni<sub>8</sub>P, Ni<sub>7</sub>P and Ni<sub>8</sub>P<sub>3</sub> are stable over the entire pressure range of 100-400 GPa and do not undergo phase transitions. Ni5P, like the aforementioned phosphides, has no phase transitions. At 100 GPa, Ni<sub>5</sub>P is a metastable phase ( $\Delta$ H =35 meV/ atom). The stability field of this phosphide relative to the isochemical mixture Ni<sub>7</sub>P + Ni<sub>3</sub>P begins at a pressure of 142 GPa and persists up to 400 GPa (Figure 8).



Figure 8 – Dependence of the enthalpy of Ni<sub>5</sub>P on the decomposition reaction to Ni<sub>7</sub>P and Ni<sub>3</sub>P

In the case of Ni<sub>3</sub>P, at 100 GPa, the structure of schreibersite (I4<sup>-</sup>), which is stable at atmospheric pressure, has an enthalpy higher than the newly found structure, which is characterized by Cmca symmetry. The transition from the Ni<sub>3</sub>P-I4<sup>-</sup>structure to Ni<sub>3</sub>P-Cmcaoccurs at a pressure of 64 GPa (Figure 9).



Figure 9 – Enthalpy dependence on pressure of Ni<sub>3</sub>P modifications Note – All dependencies are shown relative to the Ni<sub>3</sub>P-Cmca enthalpy

It is worth noting that at a pressure of 100 GPa, Ni<sub>3</sub>P-*Cmca* is a metastable phase. Ni<sub>3</sub>P-*Cmca* stabilizes above 230 GPa relative to the isochemical mixture Ni5P + Ni<sub>8</sub>P<sub>3</sub>(Figure 10).



Figure 10 – Dependence of the  $Ni_3P$  enthalpy on the decomposition into  $Ni_5P + Ni_8P_3$ 

In the pressure range of 100-400 GPa, Ni<sub>2</sub>P is represented as a structure characterized by Pnma symmetry. It is well known that the structure of transjordanite (P6<sup>-</sup>2*m*) is more stable at low pressures [43]. Experimental and theoretical studies conducted at pressures up to 50 GPa have not shown the existence of a structural phase transition [12, p. 3205]. According to our calculations, Ni<sub>2</sub>P-P6<sup>-</sup>2*m* passes into the found Ni<sub>2</sub>P-*Pnma*phase at pressures above 85 GPa (Figure 11), which does not contradict experimental data.



Figure 11 – Enthalpy dependence on pressure of Ni<sup>2</sup>P modifications Note – The dependencies are shown relative to the Ni<sub>2</sub>P-*Pnma* enthalpy

At pressures up to 223 GPa, the Ni<sub>2</sub>P-*Pnma* phase is metastable with respect to the decomposition reaction  $13Ni_2P = 3Ni_8P_3 + 2NiP_2$ . Above this pressure and up to 400 GPa, this phase is thermodynamically stable (Figure 12).

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Figure 12 – Dependence of the  $Ni_2P$  enthalpy on decomposition into  $NiP_2$  and  $Ni_8P_3$ 

During the search for stable structures, no new structures were identified for the NiP<sub>2</sub> compound. The experimentally obtained monoclinic structure of NiP<sub>2</sub>-C2/cremains stable even at high pressures up to 330 GPa. Above this pressure, NiP<sub>2</sub>-C2/cdecays into Ni<sub>2</sub>P-*Pnma* and P-P6<sub>3</sub>/*mmc*(Figure 13).



Figure 13 – Dependence of NiP<sub>2</sub> enthalpy on decomposition into Ni<sub>2</sub>P and P

All predicted structures are dynamically stable. This is evidenced by the dispersion curves of phonons calculated by us (Figure 14), which have only real frequencies, which indicates the dynamic stability of these structures.



Figure 14 - Dispersion curves of phonons of predicted nickel phosphides

The structures Ni<sub>14</sub>P, Ni<sub>12</sub>P, Ni<sub>10</sub>P, Ni<sub>8</sub>P, Ni<sub>7</sub>P, Ni<sub>5</sub>P and Ni<sub>3</sub>P are characterized by fcc packing, with Ni atoms partially replaced by P atoms [44, p. 1980]. The structure of pure Ni is also characterized by fcc packing up to 400 GPa. Thus, the proposed structures can be considered as a series of «ordered» (model) solid solutions (Ni, P). This type of isomorphism between a d-metal and a light element is atypical at atmospheric pressure. At high pressures, where elements that are typical nonmetals, such as sulfur, acquire metallic properties [45], this isomorphism becomes widespread [46,47]. An example is the isomorphic substitution of iron with sulfur, silicon and carbon in GPU and BCC structures [48]. Phosphorus atoms in the structures of model solid solutions tend to be evenly distributed over the structure without clustering or forming groups. It is worth noting that structures with a phosphorus content above ~ 15 wt.% (25 mol.%), i.e. Ni<sub>2</sub>P, Ni<sub>8</sub>P<sub>3</sub> and NiP<sub>2</sub> cannot be described by fcc packing.

For example, the Ni<sub>2</sub>P-*Pnma*nickel phosphide found is characterized by a Co<sub>2</sub>Si type structure. Nickel atoms have two unequal positions in the structure. In both positions, the Ni atoms are surrounded by five P. atoms. Phosphorus has one nonequivalent position. It is surrounded by ten Ni atoms, forming PNi<sub>10</sub>-two-lobed cubes that are interconnected along the edges and along the edges (Figure 15).



Figure 15 – Ni<sub>2</sub>P-Pnmastructure

Thus, according to the results obtained, it can be assumed that at pressures of the Earth's core 9.5 wt.% of phosphorus can be dissolved in the nickel structure without lattice deformation, and the limit of phosphorus solubility in solid Ni is  $\sim 15$  wt.%. Despite the fact that Fe and Ni have similar chemical characteristics, structures with isomorphic iron substitution in the Fe-P system have not been found. This phenomenon lies in the fact that the solubility of phosphorus in iron is much lower than in nickel, and is approximately 2.6 wt.% at atmospheric pressure [49] and 4 wt.% at a pressure of 23 GPa [50]. In addition, we believe that the high solubility of phosphorus in nickel compared to the solubility of iron will lead to the fact that the solubility of P in the alloy (Fe, Ni) will be higher than in pure Fe.

## Conclusion

As a result, calculations were carried out in this study to search for stable crystal structures in Fe-P and Ni-P systems in the pressure range of 100-400 GPa. Using the VASP software package and the USPEX algorithm, we were able to determine the stability fields for the found FexPyandNixPystructures.

A recent experimental study has shown that  $Fe_2P$ -Pnma-I is a stable phase under normal conditions, and barringerite is a high-temperature modification. Our DFT calculations are in good agreement with this study and confirm that  $Fe_2P$ -Pnma-I is a stable modification at 0 GPa.

There are some discrepancies in the experimental studies on the search for the high-pressure phase of Fe<sub>3</sub>P. In [9, p. 377], the transition from Fe3P-I4<sup>-</sup>to a new phase occurs in the pressure range of 17-30 GPa. The existence of a new phase was later confirmed in experiments by Guet al.[51]. In this work, the transition was observed at a higher pressure equal to 64 GPa. However, it should be noted that in a special experiment with a long exposure at 30 GPa, in addition to the peaks of the Fe<sub>3</sub>P-I4<sup>-</sup>structure, new peaks were observed on the X-ray. The authors assumed that the new peaks correspond to the Fe<sub>2</sub>P + Fe association. However, due to the small number of new peaks, the identification of phases was ambiguous, and it is impossible to exclude the correspondence of these new peaks to the new phase of Fe<sub>3</sub>P. This interpretation is consistent with our calculations for Fe<sub>3</sub>P. According to our data, the transition from Fe<sub>3</sub>P-I4<sup>-</sup>to Fe<sub>3</sub>P-*Cmcm* occurs at 30 GPa. In this case, the new phase observed in the experiments of Gu et al. [51, p. 300] corresponds to Fe<sub>3</sub>P-*Cmcm*.

The Fe-P system is characterized by two intermediate compounds  $Fe_2P$  and FeP under the condition of an internal core. A more jelly-like phosphidem content under this condition appears Fe<sub>2</sub>P. All these results are very important for the study of the Fe–P system as a whole.

The Ni-P system is typical for individual plants and three intermediate components Ni8P3,  $Ni_2P$  and  $NiP_2$  at 100-400 GPa. The Ni-P system is characterized by the following interactions  $Ni_{14}P$ ,  $Ni_{12}P$ ,  $Ni_{10}P$ ,  $Ni_8P$ , Ni7P,  $Ni_5P$ ,  $Ni_8P$ , and  $Ni_2P$  under the condition of the Earth's inner core. The most nickel-containing phosphide under this condition appears  $Ni_{14}P$ .

The trend of phase stability for Ni–P compounds at atmospheric pressure is presented as follows:  $Ni_5P_4 > Ni_2P > Ni_{12}P_5 > NiP > Ni_8P_3 > Ni_3P > NiP_2 > NiP_3[52]$ . With increasing pressure, this sequence changes. At the pressures of the inner core, structures with a low phosphorus content

are ordered as follows:  $Ni_8P_3 < Ni_2P < Ni_2P < Ni_5P < Ni_7P < Ni_8P < Ni_{10}P < Ni_{12}P < Ni_{12}P < Ni_{14}P$ . Among the experimentally known nickel phosphides,  $Ni_8P_3$ ,  $Ni12P_5$ ,  $Ni_5P_4$ ,  $Ni_2P$ ,  $NiP_2$  and  $NiP_3$ , only  $Ni_8P_3$  and  $NiP_2$  are stable at high pressures.

The results obtained in the course of this study are fundamental and important for further investigation of the structure and composition of the cores of the Earth and planets. The data obtained will also help identify priority areas for future research. Obtaining accurate information about the composition and structure of the Earth's inner core would contribute to a deeper understanding of the internal structure and dynamics of our planet as a whole. In addition, it is of fundamental importance for the development of models describing the processes of formation, differentiation and evolution of the Earth.

The behavior of phosphorus in Fe-Ni alloys has attracted the attention of researchers, since both elements are potentially important components of the Earth's core. In this regard, understanding the characteristics of Fe-P, Ni-P compounds at high pressures is key for subsequent research.

## The contribution of the authors:

**A.B.Bazarbek** – corresponding authorand has made a significant contribution to the development of the research concept and to the design of the structure of the article. He supervised the work of all co-authors, coordinated their activities and ensured timely completion of all stages of the work;

**A.D. Akylbekova** – the author was responsible for setting the main objectives of the study,she also took part in writing the text and agreed on the final version of the article for publication;

**G.D. Kabdrakhimova** – The author was engaged in collecting experimental and theoretical data and conducting analytical calculations. She was responsible for developing the calculation methodology and interpreting the results;

**A.Sh. Omarkhan** – She made a key contribution to the calculations on the program, and data collection. She was responsible for formulating conclusions based on the results from theoretical calculations;

**A.A. Nogai** – the author was engaged in the analysis and processing of numerical data. He completed the tasks of interpreting the results and wrote the section of the article related to the results.

#### References

1.McDonough W.F.The composition of the Earth.Compositional Model for the Earth's Core // Treatise on Geochemistry.– 2014. – Vol. 2. – P. 559-577.

2. Sun Y. Unveiling the effect of Ni on the formation and structure of Earth's inner core / Y. Sun, M. Mendelev, F. Zhang // Earth, atmospheric, and planetary scienc. – 2024. – V. 121. – P. 451-462.

3. Ni P. Planet size controls fe isotope fractionation between mantle and core / P. Ni, A. Shahar, J. Badro, J. Yang // Geophysical research letter. – 2022. – V. 49. – P. 755-762.

4. Stewart A., Schmidt M. Sulfur and phosphorus in the Earth's core: The Fe-P-S system at 23 GPa // Geophysical Research Letters. – 2007. – Vol. 34. –P. 13201-13205.

5. Gu T. et al. In situ high-pressure study of FeP: Implications for planetary cores // Physics of the Earth and Planetary Interiors. –2011. – Vol. 184. –P. 154-159.

*Л.Н. Гумилев атындагы Еуразия ұлттық университетінің ХАБАРШЫСЫ.* №3(148)/ 2024 35 Физика. Астрономия сериясы ISSN: 2616-6836. eISSN: 2663-1296 6. Dera P. et al. High-pressure polymorphism of Fe2P and its implications for meteorites and Earth's core // Geophysical Research Letters. – 2008. – Vol. 35. –P. 10301-10306.

7. Litasov K. et al. (Fe,Ni)2P allabogdanite can be an ambient pressure phase in iron meteorites // Scientific Reports. – 2020. –Vol. 10. –P. 8956-8966.

8. Scott H. et al. Equation of state and high-pressure stability of Fe3P-schreibersite: Implications for phosphorus storage in planetary cores // Geophysical Research Letters. – 2007. –Vol. 34. –P. 6302-6306.

9. Scott H. et al. P–V equation of state for Fe2P and pressure-induced phase transition in Fe3P // High Pressure Research. – 2008. –Vol. 28. –P. 375-384.

10. Li T. New insight into the structural, elastic, dynamics and thermodynamic properties of Fe3P under high pressures / T. Li, Z. Dan, T. Lu, H. Chang, L. Zhou // Vacuum. – 2021. – 221. – P. 112887-112894.

11. Okamoto H. Ni-P (Nickel-Phosphorus) // Journal of Phase Equilibria and Diffusion. – 2010. –Vol. 31. – P. 200-201.

12. Dera P. et al. Structure and behavior of the barringerite Ni end-member, Ni2P, at deep Earth conditions and implications for natural Fe-Ni phosphides in planetary cores // Journal of Geophysical Research: Solid Earth. – 2009. –Vol. 114. –P. 3201-3210.

13. Chornkrathok S., Zhang D., Dera P. Structure and Behavior of the Ni End-Member Schreibersite Ni3P under Compression to 50 GPa // Minerals. – 2020.–Vol. 10. –P. 306-309.

14. Аминова Р.М. Основы современной квантовой химии. – Казань: КГУ, 2004. – 106 с.

15. Alfe D. The ab initio treatment of high-pressure and high-temperature mineral properties and behavior // Treatise on Geophysics. –2015. –Vol. 2. –P. 369-392.

16. Bazhanova Z., Oganov A., Gianola O. Fe–C and Fe–H systems at pressures of the Earth's inner core // Physics Uspekhi. – 2012. – V. 55. – P. 489-497.

17. Bazhanova Z., Roizen V., OganovA. High-pressure behavior of the Fe–S system and composition of the Earth's inner core // Physics-Uspekhi. –2017.–Vol. 60.–P. 1025-1032.

18. Alkhaldi H., Kroll P. Computing the iron–nitrogen phase diagram at high pressure and high temperature // Journal of Alloys and Compounds. – 2021. – V. 15. – P. 1635.

19. Sagatov E., Bazarbek A., Inerbaev T. et al. Phase Relations in the Ni–S System at High Pressures from ab InitioComputations// ACS Earth and Space Chemistry. – 2021. – Vol. 5. – P. 596-603.

20. Abuov A., Inerbaev T., Abuova F., Kaptagay G. Theoretical study of the Ni–C system in the pressure range of 0–100 GPa // Bulletin of the karaganda university «physics series». – 2012. – V. 4. – P. 104.

21. Kresse G., Furthmuller J. Efficient iterative schemes for ab initio total-energy calculations using a plane-wave basis set // Physical review B. – 1996.– Vol. 54. – P. 11169-11186.

22. Kresse G., Furthmuller J. Efficiency of ab-initio total energy calculations for metals and semiconductors using a plane-wave basis set // Computational Materials Science. –1996. –Vol. 6. – P. 15-50.

23. Kresse G., Joubert D. From ultrasoft pseudopotentials to the projector augmented-wave method // Physical Review B. –1999. –Vol. 59. –P. 1758-1775.

24. Perdew J., Burke K., Ernzerhof M. Generalized gradient approximation made simple // Physical review letters. –1996. –Vol. 77. –P. 3865-3868.

25. Oganov A., Glass C. Crystal structure prediction using ab initio evolutionary techniques: Principles and applications // Journal of chemical physics. – 2006. –Vol. 124. –P. 244704-244718.

26. Monkhorst H., Pack J. Special points for Brillouin-zone integrations // Physical review B. – 1976. – Vol. 13. – P. 5188-5192.

27. Methfessel M., Paxton A. High-precision sampling for Brillouin-zone integration in metals // Physical Review B. – 1989. – Vol. 40. –P. 3616-3621.

28. Bancroft D., Peterson E., Minshall S. Polymorphism of iron at high pressure // Journal of Applied Physics. – 1956. – Vol. 27. – P. 291-298.

29. Bassett W., Huang E. Mechanism of the body-centered cubic-hexagonal close-packed phase transition in iron // Science. – 1987. – Vol. 238. – P. 780-783.

30. Rueff J. et al. Magnetic and structural  $\alpha$ -  $\epsilon$  phase transition in Fe monitored by x-ray emission spectroscopy // Physical Review B. – 1999. – Vol. 60. –P. 14510-14512.

31. Barge N., Boehler R. Effect of non-hydrostaticity on the  $\alpha$ - $\epsilon$  transition of iron // High Pressure Research. – 1990. – Vol. 6. – P. 133-140.

32. Brown A. Rundqvist S. Refinement of the crystal structure of black phosphorus // Acta Crystallographica. – 1965. – Vol. 19. – P. 684-685.

33. Jamieson J. Crystal structures adopted by black phosphorus at high pressures // Science. – 1963. – Vol. 139. – P. 1291-1292.

34. Kikegawa T., Iwasaki H. An X-ray diffraction study of lattice compression and phase transition of crystalline phosphorus // Acta Crystallographica Section B: Structural Science. – 1983. – Vol. 39. – P. 158-164.

35. Akahama Y., Kobayashi M., Kawamura H. Simple-cubic–simple-hexagonal transition in phosphorus under pressure // Physical Review B. – 1999. – Vol. 59. – P. 8520-8525.

36. Fujihisa H. et al. Incommensurate structure of phosphorus phase IV // Physical review letters. – 2007. – Vol. 98. –P. 175501-175504.

37. Marques M. et al. Origin of incommensurate modulations in the high-pressure phosphorus IV phase // Physical Review B. – 2008. – Vol. 78. –P. 54120-54128.

38. Sugimoto T. et al. Identification of superlattice structure cI16 in the P-VI phase of phosphorus at 340 GPa and room temperature via X-ray diffraction // Physical Review B. – 2012. – Vol. 86. –P. 24109-24113.

39. Okamoto H. The Fe-P (iron-phosphorus) system // Bulletin of Alloy Phase Diagrams. –1990. – Vol. 11. – P. 404-412.

40. Zaitsev A., et al. Thermodynamic properties and phase equilibria in the Fe–P system // Journal of the Chemical Society, Faraday Transactions. – 1995. – Vol. 91. – P. 703-712.

41. McMahan A., Albers R. Insulating Nickel at a Pressure of 34 TPa // Physical Review Letters. – 1982. – Vol. 49. – P. 1198-1201.

42. Inerbaev, T. M., Sagatov, N., Sagatova, D., Gavryushkin, P. N., Akilbekov, A. T., Litasov, K. D. Phase Stability in Nickel Phosphides at High Pressures // ACS Earth and Space Chemistry. -2020. – V. 4. – P. 1978–1984.

43. Nisar J., Ahuja R. Structure behavior and equation of state (EOS) of Ni2P and (Fe1–x Nix)2P (allabogdanite) from first-principles calculations // Earth and Planetary Science Letters. –2010. –Vol. 295. – P. 578-582.

44. Литасов К.Д., Шацкий А.Ф. Состав и строение ядра земли. – Новосибирск: Издательство СО РАН, 2016. – 304 с.

45. Gavryushkin P.N. et al. High-pressure phases of sulfur: Topological analysis and crystal structure prediction // Physica Status Solidi (B). – 2017. – Vol. 254. –P. 1600857-1600860.

46. Li Y., Vocadlo L., Brodholt J. The elastic properties of hcp-Fe alloys under the conditions of the Earth's inner core // Earth and Planetary Science Letters. – 2018. – Vol. 493. – P. 118-127.

47. Gavryushkin P.N. et al. Stability of B2-type FeS at Earth's inner core pressures // Geophysical Research Letters. – 2016. – Vol. 43. – P. 8435-8440.

48. Gavryushkin P. et al. Unbiased crystal structure prediction of NiSi under high pressure // Journal of Applied Crystallography. – 2015. – Vol. 48. – P. 906-908.

49. Zaitsev A., et al. Thermodynamic properties and phase equilibria in the Fe–P system // Journal of the Chemical Society, Faraday Transactions. – 1995. – Vol. 91. – P. 703-712.

50. Stewart A., Schmidt M. Sulfur and phosphorus in the Earth's core: The Fe-P-S system at 23 GPa // Geophysical Research Letters. – 2007. – Vol. 34. –P. 13201-13205.

51. Gu T. et al. High-pressure behavior of Fe3P and the role of phosphorus in planetary cores // Earth and Planetary Science Letters. – 2014.–Vol. 390. –P. 296-303.

52. Chen J. et al. Theoretical study on the phase stability, elasticity, hardness and electronic structures of Ni–P compounds // Phase Transitions. – 2016. – Vol. 89. –P. 1078-1089.

#### А.Б. Базарбек\*1, А.Д. Акылбекова1, Г.Д.Кабдрахимова1, А.Ш. Омархан1, А.А. Ногай2

<sup>1</sup>Л.Н. Гумилев атындағы Еуразия ұлттық университеті, Астана, Қазақстан <sup>2</sup>С. Сейфуллин атындағы Қазақ агротехникалық зерттеу университеті

## Темір-фосфор және никель-фосфор жүйелері үшін тұрақты құрылымдарды табудың abinitio есептеулері

**Аңдатпа.** Біздің планетамыздың ішкі құрылымын зерттеу іргелі зерттеулердегі ең өзекті тақырыптардың бірі болып табылады. Атап айтқанда, темір мен никель қосылыстарының жоғары қысымдағы жеңіл элементтермен фазалық қатынасын талдау біздің планетамыздың ядросының құрамы мен құрылымын анықтаудың маңызды міндеті болып табылады. Осындай жоғары қысымда эксперименттер жүргізудің қиындығына байланысты (Жер ядросында ~365 ГПа) Ab-initio есептеулері осындай зерттеулерді жүргізудің пайдалы әдісіне айналады.

USPEX, AIRS және CALYPSO сияқты кристалды құрылымдарды іздеудің жаңа алгоритмдерінің пайда болуымен жеңіл элементтері бар темір-никель жүйелерінің қосылыстары туралы зерттеулер мен қол жетімді деректер айтарлықтай өсті. Бұл құралдар планеталардағы ішкі процестерді зерттеудегі мүмкіндіктерімізді едәуір кеңейтіп, планеталық денелердің эволюциясын одан әрі зерттеу мен түсінудің кең перспективаларын жасады.Осы озық есептеу әдістерінің интеграциясы Жер ядросындағы материалдардың сипаттамасы туралы баға жетпес деректерді қамтамасыз ете отырып, экстремалды жағдайларда темір қосылыстарының тұрақты және метастабильді фазаларын дәл болжауға мүмкіндік береді.

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47. Gavryushkin P.N. et al. Stability of B2-type FeS at Earth's inner core pressures // Geophysical Research Letters. – 2016. – Vol. 43. – P. 8435-8440.

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#### А.Б. Базарбек\*1, А.Д. Акылбекова1, Г.Д.Кабдрахимова1, А.Ш. Омархан1, А.А. Ногай2

<sup>1</sup>Л.Н. Гумилев атындағы Еуразия ұлттық университеті, Астана, Қазақстан <sup>2</sup>С. Сейфуллин атындағы Қазақ агротехникалық зерттеу университеті

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А.Б. Базарбек<sup>\*1</sup>, А.Д. Акылбекова<sup>1</sup>, Г.Д.Кабдрахимова<sup>1</sup>, А.Ш. Омархан<sup>1</sup>, А.А. Ногай<sup>2</sup> <sup>1</sup>Евразийский национальный университет им. Л.Н. Гумилева, Астана, Казахстан <sup>2</sup>Казахский агротехнический исследовательский университет им. С. Сейфуллина

# Расчеты ab-initio для поиска стабильных структур для систем железо-фосфор и никельфосфор

Аннотация. Изучение внутреннего строения нашей планеты является одной из наиболее актуальных тем фундаментальных исследований. В частности, анализ фазовых соотношений соединений железа и никеля с легкими элементами при высоких давлениях является важной задачей для определения состава и структуры ядра нашей планеты. Из-за сложности проведения экспериментов при таких высоких давлениях (в ядре Земли ~365 ГПа) расчеты ab-initio становятся полезным методом проведения таких исследований.

С появлением новых алгоритмов поиска кристаллических структур, таких, как USPEX, AIRS и CALYPSO, количество исследований и доступных данных о соединениях железоникельсодержащих систем с легкими элементами значительно возросло. Эти инструменты значительно расширили наши возможности в изучении внутренних процессов на планетах, создав более широкие перспективы для дальнейших исследований и понимания эволюции планетных тел. Интеграция этих передовых вычислительных методов позволяет точно прогнозировать стабильные и метастабильные фазы соединений железа в экстремальных условиях, предоставляя бесценные данные о поведении материалов в условиях ядра Земли.

**Ключевые слова:** физика высокого давления, расчеты Ab-initio, квантово-химическое моделирование, фундаментальные исследования, кристаллические структуры.

## Сведения об авторах:

*Базарбек А.Б. –* хат-хабар авторы, PhD, Л.Н. Гумилев атындағы Еуразия ұлттық университетінің доцент м.а., Сәтбаев көшесі, 2, Астана, Қазақстан.

*Акылбекова А.Д.* – PhD, Л.Н. Гумилев атындағы Еуразия ұлттық университетінің доцент м.а., Сәтбаев көшесі, 2, Астана, Қазақстан.

*Кабдрахимова Г.Д.* – PhD, Л.Н. Гумилев атындағы Еуразия ұлттық университетінің доцент м.а., Сәтбаев көшесі, 2, Астана, Қазақстан.

*Омархан А.Ш.* – Л.Н. Гумилев атындағы Еуразия ұлттық университетінің докторанты, Сәтбаев көшесі, 2, Астана, Қазақстан.

*Ногай А.А.* – PhD, C. Сейфуллин атындағы Қазақ агротехникалық зерттеу университетінің аға оқытушысы, Жеңіс көшесі, 62, Астана, Қазақстан.

*Базарбек А.Б.* – автор для корреспонденции, PhD, и. о. доцента, Евразийский национальный университет им. Л. Н. Гумилева, ул. Сатпаева, 2, Астана, Казахстан.

*Акылбекова А.Д.* – PhD, и.о. доцента, Евразийский национальный университетим. Л.Н. Гумилева, ул. Сатпаева, 2, Астана, Казахстан.

*Кабдрахимова Г.Д.* – PhD, и.о. доцента, Евразийский национальный университетим. Л.Н. Гумилева, ул. Сатпаева, 2, Астана, Казахстан.

*Омархан А.Ш.* – докторант,Евразийский национальный университетим.Л. Н. Гумилева, ул. Сатпаева, 2, Астана, Казахстан.

*Ногай А.А.* – PhD, старший преподаватель, Казахский агротехнический исследовательский университет им. С. Сейфуллина, ул. Женис, 62, Астана, Казахстан.

## Information about authors:

*Bazarbek A.B.* – corresponding author, PhD, acting associate professor of L. N. Gumilyov Eurasian National University, 2 Satpayev str., Astana, Kazakhstan.

*Akylbekova A.D.* – PhD, acting associate professor of L. N. Gumilyov Eurasian National University, 2 Satpayev str., Astana, Kazakhstan.

*Kabdrakhimova G.D.* – PhD, acting associate professor of L. N. Gumilyov Eurasian National University, 2 Satpayev str., Astana, Kazakhstan.

*Omarkhan A.Sh. –* PhD student of L. N. Gumilyov Eurasian National University, 2 Satpayev str., Astana, Kazakhstan.

*Nogai A.A.* – PhD, senior lecturerof Kazakh Agro-Technical Research University, 62 Zhenis str., Astana, Kazakhstan.



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